$$\int_{\overline{f}} \overrightarrow{f} \cdot d\overrightarrow{n} = \iint_{Not} Not \overrightarrow{f} \cdot d\overrightarrow{s}$$

$$\int_{\overline{f}} \overrightarrow{f} \cdot \overrightarrow{f} ds = \iint_{S} Not \overrightarrow{f} \cdot \overrightarrow{n} ds$$

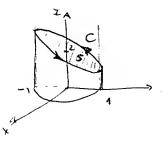
$$c$$

integral de l'una de la = integral de superficie de la componente promuel del pot = emponente promuel del pot = fronterie de S.

iourdan que 
$$\overrightarrow{T} = \frac{d\overrightarrow{r}}{\frac{dt}{dt}}$$

In other seads 
$$\frac{ds}{dt} = \frac{d\vec{r}}{dt} = \frac{d\vec{r}$$

Genific : Evalue  $\int \vec{F} \cdot d\vec{r}$ , donde  $\vec{F}(x,y,z) = -\vec{g}\hat{i} + x\hat{j} + z^2\hat{k}$  y to  $\vec{r}$  Con le surve de interfección del peano y+z=z son el silvinoleo  $x^2+y^2=1$ . (Overtade C de menero que se recurra en sen ti do contrairo al de las manea las alle seloj)



$$\int_{C} \vec{F} \cdot d\vec{r} = \iint_{C} Not \vec{F} \cdot \vec{n} ds$$

$$\text{Mod} \vec{f} = \begin{pmatrix} \hat{i} & \hat{j} & \hat{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ -\hat{j}^{2} & \times \hat{z}^{2} \end{pmatrix} = \begin{pmatrix} 0 - 0, 0 - 0, +2y, \\ 0, 0, 1 + 2y, \end{pmatrix}$$

Janeme Frica de C

x=x , y=y Z=g(x,y) Z=2-y

$$\frac{\vec{n} = \left(-\frac{36}{3x}, \frac{36}{3y}, 1\right)}{\sqrt{1 + \left(\frac{36}{3x}\right)^2 + \left(\frac{36}{3x}\right)^2}} = \frac{\left(0, -1, 1\right)}{\sqrt{1 + p + 1}} = \frac{\left(0, -1, 1\right)}{\sqrt{2}}$$

$$\int_{C} \vec{r} d\vec{r} = \iint_{C} A_{0}r + \vec{r} \cdot \vec{n} ds.$$

$$= \iint_{C} (\nabla x + \vec{r} \cdot) (O_{1} - I_{1} I) \cdot \vec{r} \cdot \vec{r} dA.$$

$$= \iint_{C} (O_{1} O_{1} I + 2y) (O_{1} + I_{1} I) dA$$

$$= \iint_{C} (1 + 2y) dA$$

En nte caro Des ele disco de radio A. y en coord. places.

$$= \int_{0}^{2\pi} \int_{0}^{1} (1 + 2\pi \sin \theta) \pi dx d\theta$$

$$= \int_{0}^{2\pi} \int_{0}^{1} (n + 2\pi \sin \theta) \pi dx d\theta$$

$$= \int_{0}^{2\pi} \left[ \frac{n^{2}}{2} + 2\frac{n^{3}}{3} \tan \theta \right] d\theta$$

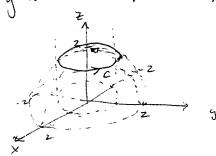
$$= \int_{0}^{2\pi} \left( \frac{1}{2} + \frac{2}{3} \sin \theta \right) d\theta$$

$$= \int_{0}^{2\pi} \left( \frac{1}{2} + \frac{2}{3} \sin \theta \right) d\theta$$

$$= \frac{1}{2} \frac{1}{2} \left( \frac{1}{2} + \frac{2}{3} \cos \theta \right) d\theta$$

$$= \frac{2\pi}{2} - \frac{2}{3} \left( \cos 2\pi - \cos \theta \right) = \pi$$

Shot F. ds donde F = (yt, xz, xy) y Su le parte de lo en ferre X<sup>2</sup>+y<sup>2</sup>+z<sup>2</sup>=4 que se encuentra dentro del cibiodro x<sup>2</sup>+y<sup>2</sup>=1 y amba del plano xy.



$$\begin{array}{c} \chi^{2} + y^{2} + z^{2} = 4 \\ \chi^{2} + y^{2} = 1 \end{array}$$

$$(+z^{2} = 4)$$

$$z^{2} = 3 \longrightarrow z = \sqrt{3} \quad (+)$$

Osí Cer el circuis dodo por X+y=1, 7=13' lo esmanión rechrid de C is

$$\vec{R}(t) = \cot 2 + \cot 3 + \sqrt{3} \hat{k}$$

$$\vec{R}'(t) = -\cot 2 + \cot 3 + 0 \hat{k}$$

F(r(t)) = 13 sent 2 + 15 wst j + cost sent 2 for el secremo de stokes

$$\int_{S}^{2\pi} \cot^{2}\theta ds = \int_{S}^{2\pi} \frac{1}{\pi} \cdot ds = \int_{S}^{2\pi} \frac{1}{\pi} (\pi t) \cdot \tilde{\chi}^{2}(t) \cdot dt$$

$$= \int_{S}^{2\pi} \left( -13 \text{ sent}, \sqrt{3} \text{ sost}, \text{ sost sent} \right) \cdot \left( -\text{sent}, \text{ cost}, 0 \right) dt$$

$$= \int_{S}^{2\pi} \left( -\sqrt{3} \text{ sen}^{2}t + \sqrt{3} \text{ cos}^{2}t \right) dt = \int_{S}^{2\pi} \left( \text{ cos}^{2}t - \text{ sen}^{2}t \right) dt$$

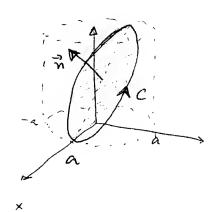
$$= \int_{S}^{2\pi} \left( -\sqrt{3} \text{ sen}^{2}t + \sqrt{3} \text{ cos}^{2}t \right) dt = 0.$$

W20 = WE-sm20

## Ejucio:

Calcular 
$$\int (y-z)dx + (z-x)dy + (x-y)dz$$
,

$$x^{2}+y^{2}=a^{2}$$
 y d plano  $\frac{x}{a}+\frac{2}{5}=1$ ;  $a,5>0$ .



## luando:

$$x = 0 \rightarrow z = 6$$

$$x = -a \longrightarrow 2 = 26$$
.

apeican stokes.

See see 5 la elépse que se produce ou intertecten lan des tuperficies. aplicamos el terrence de stokes.

$$\int_{C} \vec{F} \cdot d\vec{r} = \iint_{S} rot \vec{F} \cdot d\vec{s} = \iint_{S} (\nabla x \vec{F}) \cdot d\vec{s}$$

$$= \iint_{S} (\nabla x \vec{F}) \cdot \vec{n} ds$$

Note: 
$$\iint_{S} \overrightarrow{H} \cdot d\overrightarrow{s} = \iint_{S} \overrightarrow{H} \cdot \overrightarrow{m} ds = \iint_{S} (H_{1}, H_{2}, H_{3}) \cdot \underbrace{\left(-\frac{25}{20}, -\frac{25}{20}, 1\right)}_{\sqrt{\frac{1}{20}}} \underbrace{\left(\frac{25}{20}, \frac{25}{20}, \frac{25}{20}, 1\right)}_{\sqrt{\frac{1}{20}}} \underbrace{\left(\frac{25}{20}, \frac{25}{20}, \frac{25}{20}, \frac{25}{20}, 1\right)}_{\sqrt{\frac{1}{20}}} \underbrace{\left(\frac{25}{20}, \frac{25}{20}, \frac$$

$$\frac{\vec{m} = -\frac{\partial \vec{q}}{\partial x} \vec{l} - \frac{\partial \vec{q}}{\partial y} \vec{j} + \vec{k}}{\sqrt{(\frac{\partial \vec{q}}{\partial x})^2 + (\frac{\partial \vec{q}}{\partial y})^2 + 1}}$$

$$ds = \sqrt{\left(\frac{2}{2}\right)^2 + \left(\frac{2}{2}\right)^2 + \left(\frac{dA}{dx}\right)^2} + \sqrt{\frac{dA}{dx}} dy$$

final mento

$$\iint \overrightarrow{H} \cdot d\overrightarrow{s} = \iint (H_1, H_2, H_3) \cdot (-\frac{2g}{2\chi}, \frac{2g}{2\eta}, 1) dx dy$$

$$= \iint (-H_1, H_2, H_3) \cdot (-\frac{2g}{2\chi}, \frac{2g}{2\eta}, 1) dx dy.$$
 courk status
$$= \iint (-H_1, H_2, H_3) \cdot (-\frac{2g}{2\chi}, \frac{2g}{2\eta}, 1) dx dy.$$
 courk status

$$A = \nabla \times \overrightarrow{F} = \begin{vmatrix} 2 & 1 & 1 \\ 2 & 3 & 3 \\ 3 & 3 & 3 \\ 3 & 2 & 3 \end{vmatrix}$$

$$= \frac{2}{2y} (x-y)^{\frac{1}{2}} + \frac{2}{2y} (z-x)^{\frac{1}{2}} + \frac{2}{2z} (y-z)^{\frac{1}{2}}$$

$$= \frac{2}{2y} (x-y)^{\frac{1}{2}} + \frac{2}{2z} (z-x)^{\frac{1}{2}} + \frac{2}{2z} (y-z)^{\frac{1}{2}}$$

$$= \frac{2}{2y} (y-z)^{\frac{1}{2}} - \frac{2}{2z} (z-x)^{\frac{1}{2}} - \frac{2}{2z} (x-y)^{\frac{1}{2}}$$

$$= \frac{2}{2y} (y-z)^{\frac{1}{2}} - \frac{2}{2z} (z-x)^{\frac{1}{2}} - \frac{2}{2z} (x-y)^{\frac{1}{2}}$$

$$= \frac{2}{2y} (y-z)^{\frac{1}{2}} - \frac{2}{2z} (z-x)^{\frac{1}{2}} - \frac{2}{2z} (x-y)^{\frac{1}{2}}$$

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$$= \frac{2}{2y} (y-z)^{\frac{1}{2}} - \frac{2}{2z} (z-x)^{\frac{1}{2}} - \frac{2}{2z} (z-x)^{\frac{1}{2}}$$

$$= \frac{2}{2y} (x-y)^{\frac{1}{2}} + \frac{2}{2z} (z-x)^{\frac{1}{2}} - \frac{2}{2z} (z-x)^{\frac{1}{2}}$$

$$= \frac{2}{2y} (x-y)^{\frac{1}{2}} + \frac{2}{2z} (z-x)^{\frac{1}{2}} - \frac{2}{2z} (z-x)^{\frac{1}{2}}$$

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$$= \frac{2}{2y} (x-y)^{\frac{1}{2}} + \frac{2}{2z} (z-x)^{\frac{1}{2}} - \frac{2}{2z} (z-x)^{\frac{1}{2}}$$

$$= \frac{2}{2y} (x-y)^{\frac{1}{2}} + \frac{2}{2z} (z-x)^{\frac{1}{2}} - \frac{2}{2z} (z-x)^{\frac{1}{2}}$$

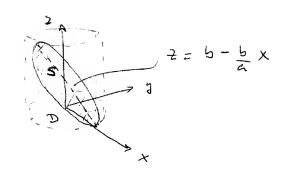
$$= \frac{2}{2y} (x-y)^{\frac{1}{2}} + \frac{2}{2z} (z-x)^{\frac{1}{2}} - \frac{2}{2z} (z-x)^{\frac{1}{2}}$$

$$= \frac{2}{2y} (x-y)^{\frac{1}{2}} + \frac{2}{2z} (z-x)^{\frac{1}{2}} - \frac{2}{2z} (z-x)^{\frac{1}{2}}$$

$$= \frac{2}{2} (x-y)^{\frac{1}{2}} + \frac{2}{2z} (z-x)^{\frac{1}{2}} - \frac{2}{2z} (z-x)^{\frac{1}{2}}$$

$$= \frac{2}{2} (x-y)^{\frac{1}{2}} + \frac{2}{2z} (z-x)^{\frac{1}{2}} - \frac{2}{2z} (z-x)^{\frac{1}{2}}$$

$$= -12 - 1\hat{k} - 1\hat{j} - 1\hat{k} - 1\hat{j} - 1\hat{k} - 1\hat{j} = (-2, -2, -2) = (H_1, H_2, H_3)$$



$$\int_{c}^{\frac{1}{2}} dx^{2} = \iint_{S} (\nabla x^{\frac{2}{2}}) dx^{2} = \iint_{S} (\nabla x^{\frac{2}{2}}) dx^{2} dx^{2} = \iint_{S} (-\frac{2b}{a} - 2) dx^{2} dy^{2} = \lim_{S \to \infty} \int_{A=0}^{2\pi} (-\frac{2b}{a} - 2) dx^{2} dx^{2} = \lim_{S \to \infty} \int_{A=0}^{2\pi} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{a} - 2) \int_{S} \frac{d}{2} dx^{2} = \lim_{S \to \infty} (-\frac{2b}{$$